

CLAIMS

1. A cryptographic method in an electronic component during which a modular exponentiation of the type x^d is performed, with d an integer exponent of $m+1$ bits, by scanning the bits of d from left to right in a loop indexed by i varying from m to 0 and calculating and storing in an accumulator (R0), at each turn of rank i , an updated partial result equal to $x^{b(i)}$, $b(i)$ being the $m-i+1$ most significant bits of the exponent d ($b(i) = d_{m \rightarrow i}$),

the method being characterised in that, at the end of a turn of rank $i(j)$ ($i = i(0)$) chosen randomly, a randomisation step E1 is performed during which:

E1: a random number z ($z = b(i(j))$, $z = b(i(j)).2^t$, $z = u$) is subtracted from a part of the bits of d not yet used ($d_{i-1 \rightarrow 0}$) in the method

then, after having used the bits of d modified by the randomisation step E1, a consolidation step E2 is performed during which:

E2: the result of the multiplication of the content of the accumulator ($x^{b(i)}$) by a number that is a function of x^z stored in a register (R1) is stored ($R0 \leftarrow R1 \times R0$) in the accumulator (R0).

2. Method according to the preceding claim, in which step E1 is repeated one or more times, at the end of various turns of rank $i(j)$ ($i = i(0)$, $i = i(1)$, ...) chosen randomly between 0 and m .

3. Method according to the preceding claim, in which, at each turn i , it is decided randomly ($p=1$) whether or not step E1 is performed.

4. A cryptographic method according to one of
 5 claims 1 to 3, in which the number z ($z=b(i(j))$, $z = b(i(j)).2^i$) is a function of the exponent d , in which, during the randomisation step, the result of the multiplication of the content of the accumulator ($x^b(i)$) by the content of the register (R1) is also
 10 stored ($R1 \leftarrow R0 \times R1$) in the said register (R1).

5. A method according to claim 4, in which the consolidation step E2 is performed after the last turn of rank i equal to 0.

6. A method according to the preceding claim,
 15 during which, during step E1, the number $b(i)$ is subtracted from d .

7. A method according to claim 6, during which the following is effected:

Input: $x, d = (d_m, \dots, d_0)_2$

20 Output: $y = x^d \bmod N$

$R0 \leftarrow 1; R1 \leftarrow 1; R2 \leftarrow x, i \leftarrow m$

as long as $i \geq 0$, do:

$R0 \leftarrow R0 \times R0 \bmod N$

if $d_i = 1$ then $R0 \leftarrow R0 \times R2 \bmod N$

25 $p \leftarrow R\{0, 1\}$

if $((p = 1) \text{ and } d_{i-1 \rightarrow 0} \geq d_{m \rightarrow i})$ then

$d \leftarrow d - d_{m \rightarrow i}$

$R1 \leftarrow R1 \times R0 \bmod N$

end if

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        i <- i-1
    end as long as
    R0 <- R0xR1 mod N
return R0

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5 8. A method according to claim 5, during which step E1 is modified as follows:

E1: a number equal to $g.b(i)$ is subtracted from d , g being a positive integer; the current partial result ($x^b(i)$) is raised to the power of g and the result is stored in the register (R1).

10 9. A method according to the preceding claim, in which g is equal to 2^τ , τ being a random number chosen between 0 and T .

15 10. A method according to the preceding, in which the following is effected:

Input: $x, d = (d_m, \dots, d_0)_2$

Output: $y = x^d \bmod N$

$R0 \leftarrow 1; R1 \leftarrow -1; R2 \leftarrow x, i \leftarrow m$

as long as $i \geq 0$, do:

20 $R0 \leftarrow R0 \times R0 \bmod N$

if $d_i = 1$ then $R0 \leftarrow R0 \times R2 \bmod N$

$p \leftarrow R\{0, 1\}; \tau \leftarrow R\{0, \dots, T\}$

if $((p = 1) \text{ and } (d_{i-1 \rightarrow \tau} \geq d_{m \rightarrow i}))$ then

$d_{i-1 \rightarrow \tau} \leftarrow d_{i-1 \rightarrow \tau} - d_{m \rightarrow i}$

25 $R3 \leftarrow R0$

as long as $(\tau > 0)$ do:

$R3 \leftarrow R3^2 \bmod N; \tau \leftarrow \tau - 1$

end as long as

$R1 \leftarrow R1 \times R3 \bmod N$

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        end if
        i <- i-1
    end as long as
    R0 <- R0xR1 mod N
5    return R0

    11. A method according to one of claims 1 to 4,
    in which the consolidation step E2 is performed at the
    end of the rank using the last bit of d modified during
    step E1.

10    12. A method according to claim 11, in the
    course of which, during step E1, the number b(i) is
    subtracted from the bits of d of rank i(j) - c(j) to
    i(j)-1, c(j) being an integer, and the content of the
    accumulator ( $x^{b(i(j))}$ ) is stored in the register (R1).

15    13. A method according to the preceding claim,
    in the course of which, during the turn of rank i(j+1),
    it is chosen randomly to perform step E1 only if  $i(j+1) \leq i(j)-c(j)$ . ( $\sigma = 1$  free semaphore).

    14. A method according to claim 12 or 13, in
20    which c(j) is equal to  $m-i(j)+1$ .

    15. A method according to the preceding claim,
    during which the following steps are performed:

    Input:  x, d =  $(d_m, \dots, d_0)_2$ 
    Output: y =  $x^d \bmod N$ 

25    R0 <- 1; R1 <-1; R2 <- x,
        i <- m; c <- -1;  $\sigma$  <- 1
        as long as  $i \geq 0$ , do:
            R0 <- R0xR0 mod N
            if  $d_i = 1$  then R0 <- R0xR2 mod N end if

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        if ( $2i \geq m+1$ ) and ( $\sigma=1$ ) then  $c \leftarrow m-i+1$ 
                                if not  $\sigma = 0$ 
        end if
         $\rho \leftarrow R\{0, 1\}$ 
5       $\varepsilon \leftarrow \rho$  and ( $d_{i-1 \rightarrow i-c} \geq d_{m \rightarrow i}$ ) and  $\sigma$ 
        if  $\varepsilon = 1$  then
             $R1 \leftarrow R0$ ;  $\sigma \leftarrow 0$ 
             $d_{i-1 \rightarrow i-c} \leftarrow d_{i-1 \rightarrow i-c} - d_{m \rightarrow i}$ 
        end if
10     if  $c = 0$  then
             $R0 \leftarrow R0 \times R1 \bmod N$ ;  $\sigma \leftarrow 1$ 
        end if
         $c \leftarrow c-1$ ;  $i \leftarrow i-1$ 
        end as long as
15     return  $R0$ 

16. A method according to claim 12 or 13, in
which  $c(j)$  is chosen randomly between  $i(j)$  and  $m-i(j)+1$ .

17. A method according to the preceding claim,
20 during which the following is effected:
    Input:  $x, d = (d_m, \dots, d_0)_2$ 
    Output:  $y = x^d \bmod N$ 
         $R0 \leftarrow 1$ ;  $R1 \leftarrow 1$ ;  $R2 \leftarrow x$ ,
         $i \leftarrow m$ ;  $c \leftarrow -1$ ;  $\sigma \leftarrow 1$ 
25     as long as  $i \geq 0$ , do:
         $R0 \leftarrow R0 \times R0 \bmod N$ 
        if  $d_i = 1$  then  $R0 \leftarrow R0 \times R2 \bmod N$ 
            if ( $2i \geq m+1$ ) and ( $\sigma = 1$ )
                then  $c \leftarrow R\{m-i+1, \dots, i\}$ 

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                                if not  $\sigma = 0$ 
                                 $\varepsilon \leftarrow \rho$  and  $(d_{i-1 \rightarrow i-c} \geq d_{m \rightarrow i})$  and  $\sigma$ 
                                if  $\varepsilon = 1$  then
                                     $R1 \leftarrow R0; \sigma \leftarrow 0$ 
5                                 $d_{i-1 \rightarrow i-c} \leftarrow d_{i-1 \rightarrow i-c} - d_{m \rightarrow i}$ 
                                end if
                                if  $c = 0$  then
                                     $R0 \leftarrow R0 \times R1 \bmod N; \sigma \leftarrow 1$ 
                                end if
10                                 $c \leftarrow c-1; i \leftarrow i-1$ 
                                end as long as
                                return  $R0$ 

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18. A method according to one of claims 1 to 2,
 in which the number z is a number u ($z = u$) of v bits
 15 chosen randomly and independent of the exponent d .

19. A method according to the preceding claim,
 in which, during step E1, the number u is subtracted
 from a packet w of v bits of d .

20. A method according to the preceding claim,
 20 during which:

- if $H(w-u) + 1 < H(w)$, it is chosen to perform a
 randomisation step E1,
- if $H(w-u) + 1 > H(w)$, it is chosen not to
 perform step E1,
- 25 • if $H(w-1) + 1 = H(w)$, it is chosen randomly to
 perform or not a randomisation step E1.

21. A method according to the preceding claim,
 during which the following is effected:

Input: $x, d = (d_m, \dots, d_0)_2$

Parameters: v, k

Output: $y = x^d \bmod N$

$R0 \leftarrow 1; R2 \leftarrow x; i \leftarrow -m; L = \{\}$

as long as $i \geq 0$, do:

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5      R0  $\leftarrow$  R0xR0 mod N
      if  $d_i = 1$  then  $R0 \leftarrow R0 \times R2 \bmod N$  end if
      if  $i = m \bmod ((m+1)/k)$  then  $\sigma \leftarrow -1$  end if
      if  $\sigma = 1$  and  $L = \{\}$  then
          s  $\leftarrow$  0: u  $\leftarrow$  R {0, ...,  $2^v-1$ };
10      R1 =  $x^u \bmod N$ 
      end if
      w  $\leftarrow$   $d_{i \rightarrow i-v+1}$ 
      h  $\leftarrow$  H(w)
      if  $w \geq u$  then  $\Delta \leftarrow w-u; h_\Delta \leftarrow 1 + H(\Delta)$ 
15      if not  $h_\Delta \leftarrow v+2$ 
      end if
      p  $\leftarrow$  R{0, 1}
      if  $[(\sigma=0) \wedge (i-v+1 \geq 0)] \wedge$ 
           $[(h > h_\Delta) \text{ or } ((p=1) \text{ and } (h=h_\Delta))]$  then
20       $d_{i \rightarrow i-v+1} \leftarrow \Delta; L \leftarrow L \cup \{i-v+1\}$ 
      end if
      if  $(i \in L)$  then
          R0  $\leftarrow$  R0xR1 mod N
          L  $\leftarrow$  L\{i}
25      end if
      i  $\leftarrow$  i-1
      end as long as
return R0

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